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Presymplectic Lagrangian systems. I. The constraint algorithm and the equivalence theorem.

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A Lagrangian system is a triple (TQ, L, Ω) , where Q is a manifold, TQ its tangent bundle, L a real-valued function on TQ (the Lagrangian), and Ω the presymplectic 2-form on TQ defined in canonical coordinates (q^i, v^i) on TQ by $\Omega = (\partial^2 L / \partial v^i \partial q^j) \cdot dq^i \wedge dq^j + (\partial^2 L / \partial v^i \partial v^j) \cdot dq^i \wedge dv^j$. A special Hamiltonian system is a triple (M_1, H_1, ω_1) , where $M \subset TQ$ is a submanifold, H_1 a real-valued function on M_1 (the Hamiltonian), and ω_1 a presymplectic form on M . The authors prove the following equivalence theorem. Let (TQ, L, Ω) be an almost regular Lagrangian system, $FL: TQ \rightarrow T^*Q$ the Legendre transformation defined by L ; then (1) there exists a special Hamiltonian formulation $(FL(TQ), H_1, \omega_1)$ of the dynamics of the system, and (2) the Lagrangian and Hamiltonian formulations are equivalent. The proof is based on a constraint algorithm given by the authors and G. Hinds [*J. Math. Phys.* **19** (1978), no. 11, 2388–2399; [MR0506712 \(80e:58025\)](#)].

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